

The Crystal Structure of Calcium Thymidylate

BY K. N. TRUEBLOOD

University of California, Los Angeles 24, California, U.S.A.

AND P. HORN AND V. LUZZATI

Centre de Recherches sur les Macromolécules, Strasbourg, France

(Received 9 June 1960)

Crystals of the hexahydrate of calcium thymidylate, $C_{10}H_{13}O_8N_2CaP \cdot 6H_2O$, are monoclinic, with

$$a_0 = 14.40 \pm 0.02, \quad b_0 = 6.87 \pm 0.01, \quad c_0 = 9.81 \pm 0.01 \text{ \AA}, \quad \beta = 90^\circ 58' \pm 3'$$

The space group is $P2_1$, with one formula weight comprising the asymmetric unit. The structure was solved by analysis of a sharpened three-dimensional Patterson function and was refined by Fourier and least squares methods. During the early stages of refinement strong correlations were noted between errors in position parameters and the apparent values of corresponding vibration parameters. After seven least squares cycles, as apparent convergence was being approached, it was discovered that the sign of one of the eighty-four position parameters (for one of the water molecules) was wrong; when it was corrected, changes of as much as three e.s.d. occurred at once in bond distances not involving the wrongly placed atom. Refinement was completed with five more least squares cycles. The final e.s.d.'s of bond distances vary from 0.011 Å for the Ca–O and P–O bonds to an average of 0.023 Å for the C–C distances; for the bond angles, e.s.d.'s vary from 0.7 to 1.4°.

The six atoms of the pyrimidine ring are planar, with the four attached atoms (which occur in adjacent pairs) alternately above and below the plane of the ring by 0.05–0.10 Å. These displacements, and even more the significant distortions of the corresponding extra-ring angles, increase the distances between the atoms in these two pairs by about 0.1 Å. The deoxyribose ring is puckered, with C3' 0.53 Å from the plane of the other four atoms. The phosphate group has about the expected dimensions; the P–O ester bond is 0.07 Å longer than any of the other P–O bonds. The environment of the calcium ion is much like that in $CaHPO_4$, a distorted pentagonal bipyramid, with two water molecules on the axis and four phosphate oxygens (from three different molecules) and one water molecule in the central plane. The entire structure is held together by the Ca–O bonds and a complex network of hydrogen bonds; all but one of the fourteen hydrogen atoms which might participate in hydrogen bonding appears to do so, although the precision of the determination is not sufficient to permit unambiguous location of all the hydrogen atoms.

The deoxyribose ring makes an angle of 75° with the plane of the thymine nucleus. The conformation of the thymidylate about the glycosidic C–N bond is intermediate between that in the DNA model of Crick & Watson (1954) and that suggested by Langridge *et al.* (1957); the latter two models differ by about 70° in this conformational parameter. The disposition of the C5'–O5'–PO₃ chain is much like that in the model of Langridge *et al.*, although it appears that there would not be an appreciable energy barrier to rotation of this group to other positions. The planes of the thymine nuclei in adjacent molecules along the screw axis are about 12° from a parallel orientation, with the average spacing between them 3.4 Å, and the closest approach 3.20 Å.

The general pattern of anisotropic thermal vibrations deduced from the analysis is reasonable in terms of the packing and orientation of the components of the structure, but absorption errors in the data prevented any precise detailed analysis of thermal anisotropies.

Introduction

The key role of deoxyribonucleic acid (DNA) in the storage and transport of genetic information has focussed a great deal of effort in recent years on the elucidation of its molecular structure. The complexity of the material and the fact that it gives only fibre diffraction patterns have precluded the use of the usual single-crystal X-ray methods of structure analysis and refinement. Consequently the approach adopted has been that of attempting to construct plausible models which are in accord with the known

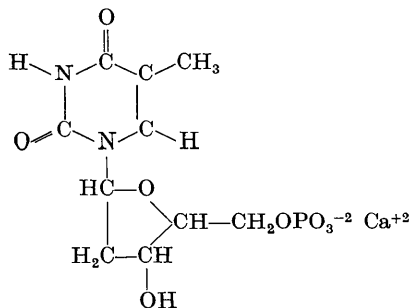
physical, chemical, and, if possible, biological properties of DNA. Several early suggestions culminated in the ingenious double-helix model proposed by Watson & Crick (1953); Crick & Watson (1954), which not only fitted remarkably well the facts known at that time but which has been supported by almost all the evidence on DNA accumulated since. However, as Crick (1957) and others have stated, further elaboration, modification, and understanding of the model must await the accumulation of additional basic physical chemical information, including precise data

on the intra- and inter-molecular geometry to be expected in polynucleotides.

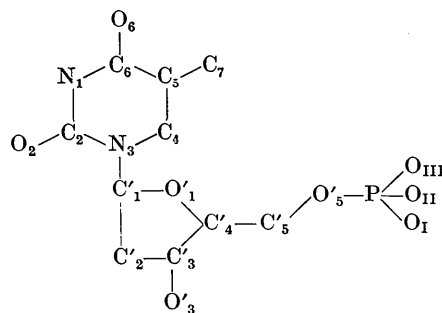
Although there have been about fifteen structure determinations of individual purines and pyrimidines reported, there have been only four of nucleosides (cytidine, Furberg, 1950; 2':3'-isopropylidene, 3:5'-cycloadenosine, Zussman, 1953; 5'-bromo-3':5'-di-deoxythymidine, Woolfson, 1956; 5'-bromo-5'-deoxythymidine, Huber, 1957), and three of nucleotides (adenylic acid, Brown *et al.*, 1953; cytidylic acid *b*, Alver & Furberg, 1957; vitamin B₁₂, Hodgkin *et al.*, 1956, 1957). Furthermore, of these last seven determinations, only that of vitamin B₁₂ was three-dimensional, and its precision was low because of the large number of atoms involved; in addition, it has the α -configuration at the glycosidic linkage, while all nucleic acid derivatives appear to be β . The only precise published study of the phosphate diester linkage, an important grouping in polynucleotides, is the structure analysis of dibenzyl phosphoric acid (Dunitz & Rollett, 1956). Spencer (1959*a*) has critically summarized the available structural information on the components of and atomic groupings in DNA and has underscored the need for precise structural studies which can define better the range of likely variation in the geometrical parameters of a polynucleotide double-helix.

The present study was undertaken with the object of providing the first structural information on the mutual arrangement of the phosphate, the sugar, and the base in a deoxyribonucleotide. Hydrated calcium thymidylate proved to be very amenable to three-dimensional structure analysis; the calcium and phosphorus atoms were easily found in the Patterson function, and were at once sufficiently heavy to make the structure determination fairly straightforward but not so heavy that they greatly limited the precision in the location of the carbon, nitrogen, and oxygen atoms. The structure has been refined to the ultimate precision that the experimental data warrant.

The molecular formula of calcium thymidylate and the atomic numbering* which we shall follow here are:



* The numbering which we have adopted for the pyrimidine ring differs from that recommended by Chemical Abstracts but is in common use and, because of its similarity to the scheme used for numbering purines, seems preferable to the C.A. system when comparisons between pyrimidines and purines are to be made. Such comparisons are frequent in consideration of nucleic acid models.



The crystal contains (according to the results of the structure determination) six water molecules in the asymmetric unit; these will be designated W1, . . . , W6.

Experimental data and procedures

All experimental work with the crystals was done at Strasbourg. Calcium thymidylate was obtained from the California Foundation for Biochemical Research and was recrystallized by slow evaporation of aqueous solutions. The thin plates which formed were elongated along *b*; *a** was normal to the principal faces of the plates.

Weissenberg and precession photographs with Ni-filtered Cu *K* α radiation showed the crystals to be monoclinic. The only systematic extinctions were (*0k0*) absent with *k* odd, which indicated that the space group is *P*2₁; the group *P*2₁/*m* is incompatible with the optical activity of the thymidylate ion. Unit cell dimensions were measured on equatorial Weissenberg photographs about *b* and *c* which had been superposed on the diffraction pattern of an aluminum wire; they are

$$a_0 = 14.40 \pm 0.02, \quad b_0 = 6.87 \pm 0.01, \quad c_0 = 9.81 \pm 0.01 \text{ \AA}; \\ \beta = 90^\circ 58' \pm 3'.$$

The density of the crystals, measured in a mixture of 'Freon 113' and bromoform was between 1.58 and 1.61 g.cm.⁻³; the density calculated for a unit cell containing two molecules of calcium thymidylate and twelve water molecules is 1.60, and thus the asymmetric unit consists of one calcium ion, one thymidylate ion, and six water molecules. (If there were only five water molecules in the asymmetric unit, the density would be 1.54; if there were seven, it would be 1.66.)

The intensities were recorded on two series of equi-inclination Weissenberg photos. For the layers *k*=0 through 5 we used a crystal of dimensions about 1.5 mm. along *b**, 0.2 mm. along *a**, and 0.5 mm. along *c**; for layers *l*=0 through 8 a smaller fragment, about 0.5 by 0.2 by 0.5 mm. was used. Each photograph was taken on four superposed Kodak Kodirex films and in most cases several different exposure times were used for each layer. Intensities were determined with a microdensitometer by measuring the density in the central region of each spot, without

integration but with correction for the error due to the separation of $K\alpha_1$ and $K\alpha_2$. Film factors were measured directly for each series of photographs. After the usual geometrical corrections had been applied, the corrected intensities were brought to a common scale by consideration of the reflections which occurred on both sets of films. An arbitrary limit was set at $\sin \theta = 0.91$; of the 1786 possible reflections within this limit, 1575 gave a measurable intensity.

No absorption corrections were made. Absorption very likely constitutes the most important source of error in the intensities; the linear absorption coefficient for $\text{Cu } K\alpha$ radiation is about 44 cm^{-1} . An approximate calculation indicates that in the most unfavorable cases variations in absorption could introduce variations in the relative values of the recorded intensities of between 2.5 and 3, and thus variations in relative F 's up to a factor of 1.7. The average variation due to absorption will of course be considerably smaller but one must expect a systematic effect with $\sin \theta$ which is formally equivalent to a negative temperature factor. Thus the thermal vibration parameters derived from these data are probably smaller than the true values.

Preliminary two-dimensional calculations were done with the von Eller photosummation device and with Beevers-Lipson strips, and corresponding structure factor calculations were made for us by La Compagnie BULL, Paris. All subsequent calculations were made on the computer SWAC (Sparks, Prosen, Kruse & Trueblood, 1956). The form factors used for oxygen, nitrogen, and hydrogen were those of McWeeny (1951), that for carbon was McWeeny's (1954) diamond curve, and that for phosphorus was taken from the *Internationale Tabellen* (1935). The scattering curve for the calcium ion was approximated by using the curve for the neutral calcium atom (Berghuis *et al.*, 1955) above $\sin \theta/\lambda = 0.2$ and by extrapolating this curve smoothly to $Z = 18$ below this value.

Determination and refinement of the structure

Consideration of a Patterson projection on (010) and of certain features of the intensity distribution on different layers about b led to rather good x and z parameters for the calcium atom and the phosphate group, and indicated approximate positions and orientations for the sugar and the base. However, many attempts to interpret Fourier projections calculated with signs based on positions derived from this Patterson distribution proved fruitless; the usual iterative procedures led nowhere. We believe in retrospect that this failure was due primarily to the absence of the water molecules from these calculations. Fig. 1 shows the relation of this first trial structure to the final structure; the mean error in the position of the calcium atom and the phosphate group was only about 0.14 \AA , that for the atoms of the sugar was about 0.5 \AA ,

and that for the thymine residue was considerably more than 1 \AA .

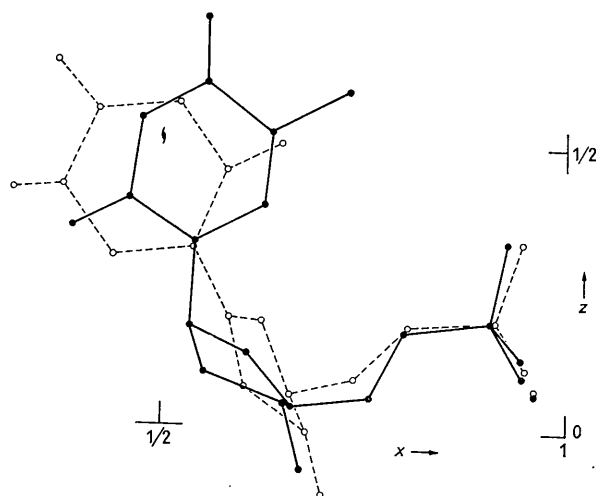


Fig. 1. Comparison of the first trial structure deduced from the Patterson projection on (010) (—○—) with the final refined structure (—●—). Water molecules have been omitted.

A sharpened three-dimensional Patterson function, with the origin peak approximately removed, was then calculated. The sharpening function by which the observed F^2 -values were divided was $\sum_i f_i^2 \exp(-5s^2)$, where $s = \sin \theta/\lambda$ and the summation is over all atoms in the unit cell. (Actually the summation included only four water molecules, rather than the twelve actually present in the unit cell, because of doubts about the number; however, this made no significant difference in the effectiveness of the sharpening, although it did affect the absolute scale slightly.) The average sharpened F^2 was then subtracted from each sharpened value and all were multiplied by a modification function (Waser, 1944) to insure convergence. The modification function was $s^4 \exp(-19s^2)$, which put maximum weight on the data at $s = 0.32$, in the middle of the $\text{Cu } K\alpha$ range.

The strongest peaks in the three-dimensional Patterson map were, as expected, those due to Ca-Ca and Ca-P interactions, and it was immediately possible to deduce coordinates not only for the calcium and phosphorus atoms but also for all of the phosphate oxygens. From the heights of the various identified peaks, it was possible to estimate the approximate height expected for a P-C interaction. The vector convergence or superposition method (Beevers & Robertson, 1950) was then applied, using the known positions of the calcium and phosphorus atoms, and admitting overlaps only for regions of Patterson density of at least the height expected for a P-C interaction. The success of this technique was striking; every atom of the calcium thymidylate molecule was located and in addition about ten possible positions were found for the six water molecules believed to be present in the asymmetric unit.

There was one significant source of ambiguity in the analysis of the vector map. The packing of the molecules is such that the calcium and phosphorus atoms have very nearly the same y -parameters. This means that the distribution of these two atoms has the symmetry of $P2_1/m$, not just $P2_1$, and consequently calculations based on this distribution have a false mirror plane perpendicular to \mathbf{b} . Thus there was an ambiguity in the choice of the sign of y for the other atoms. One sign could be chosen arbitrarily, with the others for atoms within the molecule then dictated by chemical and stereochemical considerations; since in this molecule there is a known absolute configuration, even the arbitrariness of the first choice was eventually removed. However, it was more difficult to decide upon the proper choice of a sign for y for the water molecules, particularly since there were more plausible positions than there were water molecules. On the basis of the Patterson analysis, positions were assigned tentatively to seven water molecules.

While the Patterson superposition diagram was being made, a crude approximation to the electron density, $\rho_1(xyz)$, was calculated with the observed structure factor amplitudes and phases based on the positions deduced from the Patterson for the calcium atom, the phosphorus atom, and the four phosphate oxygens. This distribution also had a false mirror plane normal to \mathbf{b} inasmuch as the phosphate group is oriented in such a way that two of the oxygen atoms lie approximately in the plane of the calcium and phosphorus atoms, and the other two are equally displaced above and below this plane and have about the same x and z coordinates. When this false symmetry was taken into account, comparison of this distribution with the results of the Patterson analysis indicated that the positions chosen for all of the atoms in the molecule and for four of the seven water molecules were plausible. However, the density at the positions suggested for each of the other three possible water molecules was very low.

A centrosymmetric Fourier projection, $\rho_1(xz)$, with signs based on the postulated positions of all twenty-nine atoms, was then calculated. It indicated that two of these three doubtful water molecules were indeed spurious, while the other one, and all of the remaining atoms, looked reasonable. Improved x and z parameters were estimated for about two-thirds of the atoms, those which were resolved in this projection, and a three-dimensional Fourier synthesis, $\rho_2(xyz)$ was then calculated with phases based on the positions of the twenty-two atoms of the molecule and the five accepted water molecules. No trace of either of the two spurious water molecules remained, but a peak of about one-half the height expected for an atom not included in the phasing appeared at a plausible position for a sixth water molecule; as indicated below, this molecule was later confirmed and included in the calculations.

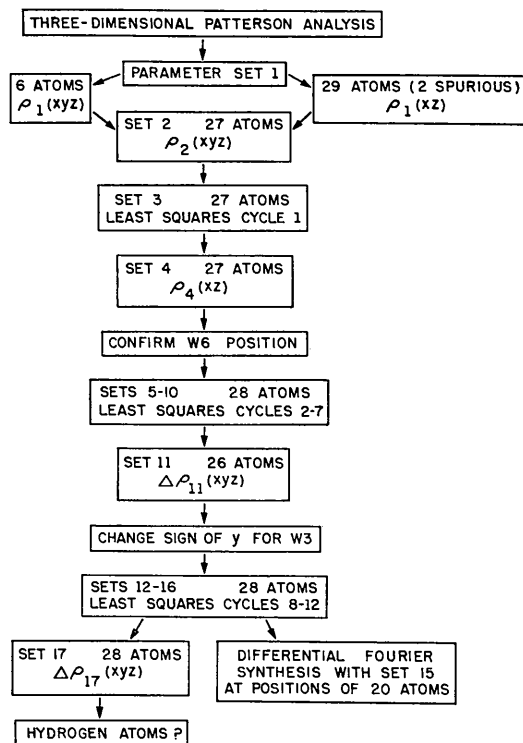


Fig. 2. Outline of the refinement stages and procedures discussed in the text.

The various stages in the refinement of the structure are outlined in Fig. 2. Least squares refinement was begun with the atomic positions estimated from ρ_2 for the entire molecule of calcium thymidylate and the five water molecules accepted at that stage (W1 to W5). Because it was known that many of these atomic positions were very crude, no attempt was made to refine temperature factors in the first two least squares cycles. The initial temperature factors were chosen after a comparison of the early calculated structure factor amplitudes with those observed, and were 1.5 \AA^2 for Ca and P, and 2.0 \AA^2 for all other atoms. The weighting scheme used throughout the least squares procedure was (with $\bar{F}_{\min.} = 4.8$):

$$F_o \geq 4\bar{F}_{\min.}, \quad |w = 4\bar{F}_{\min.}/F_o; \quad F_o \leq 4\bar{F}_{\min.}, \quad |w = 1.$$

In the early least squares cycles, the unobserved reflections were included with $F_o = 0.71F_{\min.}$ (Hamilton, 1955) and $F_{\min.}$ varying significantly in different regions of reciprocal space. In the final five refinement cycles, they were omitted because the corresponding residuals were then comparable in magnitude to those of the observed reflections (rather than appreciably smaller), and because it was not convenient to weight them appropriately (Hamilton, 1955). However, the structure factors for these reflections were calculated at each stage, as also were the terms in the

matrix of the normal equations. Even though the latter were not included in the later cycles, their effect was usually calculated; at most they would have changed bond distances and angles by less than 0.01 Å and 1° in any cycle, which is less than the e.s.d. of these quantities, although of course cumulative effects might have been slightly larger. It was also noted that inclusion of the unobserved reflections would not have significantly affected the error estimates.

The presence of so many independent atoms in the structure made it impractical to calculate and solve the full matrix of the least squares normal equations. Instead individual 3×3 and 6×6 matrices, corresponding respectively to the position parameters and anisotropic temperature parameters, were calculated and solved for each atom (Sparks, Prosen, Kruse & Trueblood, 1956). The scale factor was changed only in the first few cycles, when the temperature factors were held constant at about their average values. The shifts called for in the scale factor in later cycles were generally less than 2%; thus the scale factor appeared to be approximately correct and since no cross-terms between it and the temperature factors were calculated, it was held constant thereafter. Because interatomic cross-terms were ignored, the full shifts called for in the position and temperature factors were seldom applied; the position parameters were usually shifted by $\frac{2}{3}$ or $\frac{3}{4}$ of the indicated amount, the temperature factors by $\frac{1}{3}$ or $\frac{2}{3}$ of that calculated. Convergence was slow for various reasons—because the interatomic cross-terms were ignored, because there were so many atoms present, and because the initial structure was rather crude, nine of the atoms being displaced more than 0.2 Å from their correct positions even after one least squares cycle.

After the first cycle of least squares, calculation of a Fourier projection ($\rho_4(xz)$) strongly confirmed the existence of the sixth water molecule, W6, which had first appeared as a weak peak in ρ_2 . Six successive least squares cycles (cycles 2 through 7) were then calculated with all 28 atoms included. A careful check on the changes in various direct and derived parameters of the structure was made at each stage—the position and vibration parameters, interatomic distances, individual values of $\Delta|F|$, R , and the sum of the weighted squares of the residuals. After cycles 6 and 7 (parameter sets 10 and 11 respectively) we became very suspicious of the position of one of the water oxygen atoms, W3; not only did it have two very short apparent intermolecular contacts with other oxygen atoms (2.35 and 2.39 Å) but its apparent temperature factors continued to increase steadily, although the average value at this stage (about 8 Å²) was not impossibly large. Rossmann, Jacobson, Hirshfeld & Lipscomb (1959) have pointed out that when atoms are incorrectly placed in a structure and an attempt is made to refine their temperature factors, the latter will tend to increase to very large values. Hand calculation of the effect of atom W3 on $\Delta|F|$ for a few

of the reflections showing the greatest discrepancies between $|F_o|$ and $|F_c|$ added credence to the suspicions. Hence a difference map ($\Delta\rho_{11}$) was calculated, with the contribution of W3, and also of W2, omitted from the phasing and from the calculation of F_c . W2 was omitted partly as a control and partly because its temperature factors had also shown fairly regular increases, although the average value had reached only about 5.4 Å².

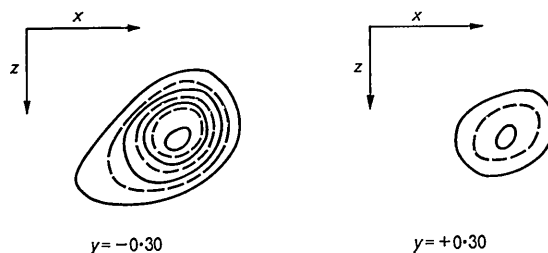


Fig. 3. Sections of $\Delta\rho_{11}$ near x and z of atom W3; y had been believed to be about 0.30. Contours start at 1 e.Å⁻³; the interval is $\frac{1}{2}$ e.Å⁻³.

In this acentric structure, a real atom omitted from the phasing should appear at about half its normal height (Luzzati, 1953; Hodgkin *et al.*, 1959) and W3 did so appear in $\Delta\rho_{11}$ at about $x, -y, z$, where x, y , and z represent the coordinates assigned to the atom previously. Pertinent regions of the map are illustrated in Fig. 3. Because the values of x and z had been approximately correct, the projections on (010) calculated earlier had been correct. It will be recalled that there had been some ambiguities about the assignment of signs to y -coordinates at the start of the analysis so that this incorrect sign for y of W3 was not surprising. Inspection of the difference map indicated that the position of W2 was correct; a peak of about the expected height (3.6 e.Å⁻³) occurred at the expected position, although there was also a small ghost peak (1.6 e.Å⁻³) at the position with the sign of y reversed. That the latter peak and the corresponding ghost of W3 were not due to disorder of W2 and W3 was shown by the fact that they were completely absent from the final difference map, $\Delta\rho_{17}$, calculated after further refinement.

Least squares cycle 8 was then calculated. The change in the sign of y for atom W3 led to distinct improvements in R , in the sum of the weighted squares of the residuals, and in a number of the bond distances within the molecule. These are apparent as the discontinuities in the curves of Figs. 4 and 5. These figures illustrate the dangers of this sort of systematic error: a number of the bond distances, none of them involving W3, changed by appreciable amounts (as much as 3σ) when this change was made in the sign of one of the eighty-four position parameters. Furthermore the changes were usually dramatically larger than the changes in the last few cycles before the correction. It is clear that if this correction had never been made,

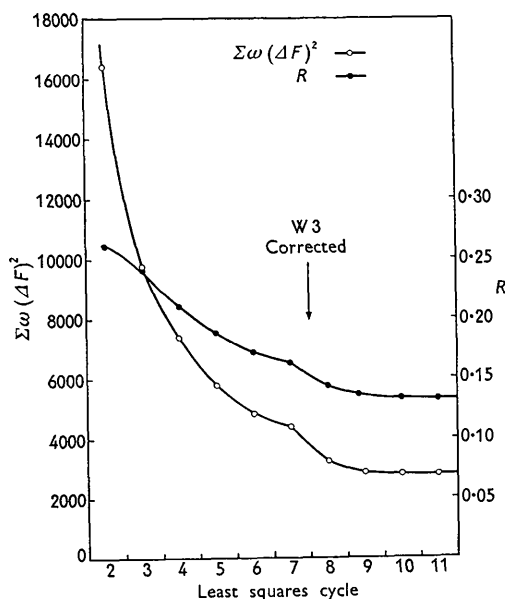


Fig. 4. Values of R (solid circles) and the sum of the weighted squares of the residuals (open circles) at successive least-squares refinement stages.

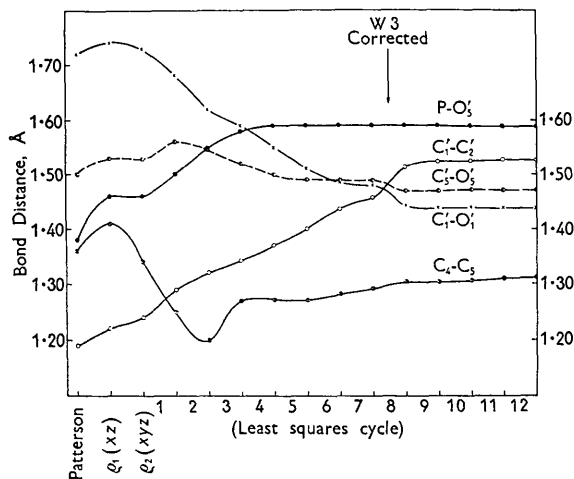


Fig. 5. Apparent values of representative bond distances at different refinement stages.

the sum of the weighted squares of the residuals would have levelled off at a value only about 20–30% higher than that finally reached, and thus the estimates of 'random errors' would have been only 10–15% higher than those we accept. Yet three of the eighteen bond distances involving C, N and O atoms would have been in error by more than 2σ from this cause alone.

Fig. 6 illustrates the overshifting of the temperature factor parameter for that atom when the position parameter for that atom is grossly in error. The sign of y for atom O_{III} was incorrectly chosen at first, but the value of y is sufficiently close to zero for this atom that the refinement moved the atom the needed

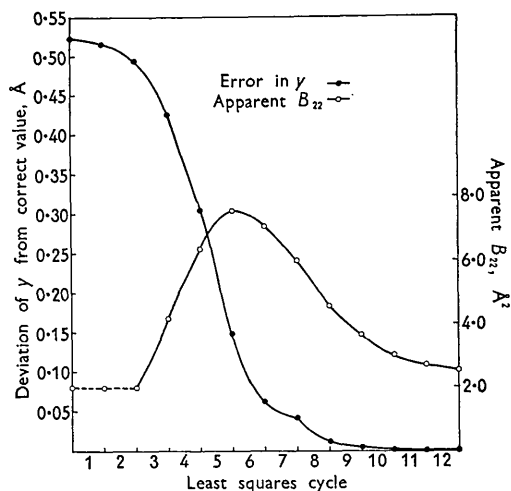


Fig. 6. Correlation between apparent temperature factor B_{22} and deviation of y from true value for atom O_{III} at successive least-squares refinement stages.

distance (about 0.55 Å) to the correct position. The apparent vibration parameter parallel to b increased markedly as long as y was far from its correct value, then decreased again to a value not far from that originally assumed to be correct. This effect has also been cited by Rossmann *et al.* (1959), who pointed out that it can be used to accelerate refinement. The difficulty with this suggestion is, of course, that it is hard in the early stages to know whether the atom is a real one far from its correct position or is entirely spurious. In any event, it is clear from the examples of W3 and O_{III} that in analyses of complex structures by least squares it is imperative to follow closely the details of the changes of parameters and apparent molecular geometry and packing at every stage.

The conclusion of the refinement was straightforward. Four more cycles of least squares refinement (9 through 12) led to parameter set 17, which was used in the calculation of a final three-dimensional difference map, $\Delta\rho_{17}$. The largest shift in position in the last squares cycle was 0.009 Å for W2; within the molecule itself, the largest shift was 0.004 Å, the average only 0.002 Å. The final difference map showed no trace of the ghost peaks of atoms W2 and W3 which had been present in $\Delta\rho_{11}$. It was possible to find peaks, or at least regions of positive density, at positions corresponding to plausible positions for all twenty-five hydrogen atoms of the asymmetric unit, thirteen in the molecule of calcium thymidylate and twelve on the six water-oxygens, W1 through W6. However, the location of these hydrogens was by no means unambiguous; there were several peaks in $\Delta\rho_{17}$ of height up to 0.7 e.Å⁻³ which, from geometrical considerations, could not possibly be identified as hydrogen atoms. This suggested strongly that the background fluctuations of the electron density caused by inadequacies of the experimental data were so great that location

of the hydrogen atoms from peak height evidence alone would be very uncertain. An estimate of the e.s.d. of the electron density from a consideration of these fluctuations gave a value of $\sigma(\rho)$ of about $0.24 \text{ e.}\text{\AA}^{-3}$; an independent calculation using the approximation $\sigma(\rho) = (1/V)[\Sigma(\Delta|F|)^2]^{1/2}$ (Cruickshank, 1949) gave $\sigma(\rho) = 0.26 \text{ e.}\text{\AA}^{-3}$. Since in this asymmetric structure hydrogen atoms omitted from the phasing are expected at peak heights of only about $0.3\text{--}0.4 \text{ e.}\text{\AA}^{-3}$, it is not surprising that many of them are partially obscured by the background.

Our selection of hydrogen positions was based upon a detailed examination of the difference map and consideration of the molecular geometry expected for both covalent and hydrogen bonding. The average density at the sites chosen is $0.33 \text{ e.}\text{\AA}^{-3}$, with sixteen of the twenty-five supposed hydrogen atoms having densities between 0.3 and $0.4 \text{ e.}\text{\AA}^{-3}$. The others range from 0.15 to $0.6 \text{ e.}\text{\AA}^{-3}$ (Table 2). The average X-H distance is $1.07 \pm 0.04 \text{ \AA}$, and the average Y-X-H bond angle $111 \pm 6^\circ$. Thus the positions are plausible geometrically and are consistent with the difference map. Furthermore their inclusion improves the agree-

Table 2. *Suggested hydrogen positions**

Atom to which H is attached		<i>x</i>	<i>y</i>	<i>z</i>	$\Delta\rho_{17} (\text{e.}\text{\AA}^{-3})$
N1	**	590	178	407	0.15
C4		317	133	683	0.3
C7	(a)	267	067	340	0.35
	(b)	275	315	340	0.4
	(c)	217	200	475	0.2
C1'		533	033	867	0.2
C2'	(a)	488	321	994	0.3
	(b)	450	433	873	0.35
C3'		293	316	887	0.4
C4'		383	020	067	0.6
C5'	(a)	245	-200	983	0.35
	(b)	195	009	024	0.2
O ₃ '	**	367	300	160	0.3
W1	(a)	120	550	620	0.4
	(b)**	117	315	700	0.4
W2	(a)**	240	630	700	0.3
	(b)	317	800	700	0.4
W3	(a)	063	-190	590	0.2
	(b)	000	-300	450	0.4
W4	(a)**	050	167	267	0.4
	(b)	142	-030	267	0.35
W5	(a)**	230	500	067	0.2
	(b)	167	540	217	0.5
W6	(a)	267	-300	333	0.2
	(b)	150	-295	405	0.4

* These positions have been chosen to be consistent with the final difference map and with a plausible molecular geometry. They cannot be considered definitely established; those marked with ** are the most ambiguous. The electron density listed is that at the suggested position in the final difference map; this was not always the maximum density of the peak. Each *x*, *y* and *z* has been multiplied by 10^3 .

Table 1. *Final atomic parameters**

Atom	<i>x</i>	<i>y</i>	<i>z</i>	$\bar{B} (\text{\AA}^2)$	$\rho_{\text{max.}} (\text{e.}\text{\AA}^{-3})$	
					Obs.	Calc.
N1	5287	1630	4664	2.3 <i>b</i>	11.7	11.0
C2	5386	1436	6056	1.8 <i>b</i>	10.1	9.7
N3	4580	1346	6766	1.8 <i>b</i>	12.6	12.0
C4	3734	1517	6126	2.0 <i>b</i>	9.6	9.1
C5	3629	1701	4803	1.8	10.0	9.5
C6	4435	1790	3936	1.5 <i>a, b</i>	10.4	9.9
O2	6171	1458	6614	3.6 <i>b</i>	12.0	11.3
O6	4463	1873	2697	2.7 <i>b</i>	13.0	12.2
C7	2694	1923	4063	3.0 <i>b</i>	8.2	7.9
C1'	4654	1065	8245	1.4 <i>b</i>	9.8	9.4
C2'	4480	2886	9094	2.1 <i>b</i>	8.8	8.6
C3'	3474	2593	9594	1.4 <i>b</i>	10.2	10.0
C4'	3417	0431	9701	1.1 <i>a, c</i>	10.9	10.7
C5'	2453	-0482	9586	1.9	9.0	8.7
O1'	3966	-0349	8613	1.6 <i>a, c</i>	15.2	14.7
O3'	3274	3570	0817	2.7	13.1	12.6
O5'	2015	0088	8280	2.0	13.5	12.8
P	0915	0079	8150	1.0 <i>a, c</i>	—	—
O _I	0580	-1787	8731	1.4 <i>a, c</i>	14.9	14.8
O _{II}	0553	1667	9071	1.6 <i>a, c</i>	14.8	14.6
O _{III}	0762	0441	6683	2.0 <i>a, b</i>	14.0	13.7
Ca	0383	4953	9340	1.0 <i>a, c</i>	—	—
W1	1326	4563	7154	2.9	—	—
W2	3104	6505	6867	7.4	—	—
W3	0538	-3013	5244	5.4	—	—
W4	0852	0285	2252	3.5	—	—
W5	1567	4982	1034	4.0 <i>b, c</i>	—	—
W6	1934	-2748	3333	4.6	—	—

* The position parameters are those of Set 17. The 'temperature factors' are average values; the letters after them represent approximate directions of maximum vibration when the individual *B*'s varied by more than a factor of 2, i.e., when the apparent vibration amplitudes varied by about 1.4. The electron densities are those evaluated in the differential Fourier synthesis with parameter Set 15; no calculations were made at that stage for the calcium, phosphorus, or water oxygen atoms. Each *x*, *y* and *z* has been multiplied by 10^4 .

ment between observed and calculated structure factor amplitudes: for the 316 observed reflections with $\sin \theta \leq 0.500$, *R* is 14.9% without inclusion of the hydrogen atoms and 14.1% when they are included. (In this calculation, $B = 5 \text{ \AA}^2$ for each of the H-atoms on a water molecule and 3 \AA^2 for the other hydrogens.) It seems clear that many of the suggested hydrogen atom positions correspond to the approximate sites of hydrogen atoms in the structure, but some of the positions certainly may be spurious, particularly on some of the water molecules.

The final position parameters (Set 17) for all the non-hydrogen atoms in the structure are given in Table 1, and those suggested for the hydrogen atoms are in Table 2. Because of the appreciable uncorrected absorption errors, the final values of the anisotropic temperature factors resulting from the least squares procedure were somewhat erratic, and we do not feel that the detailed anisotropies indicated by them are of much significance. Consequently we have merely indicated average values of *B* for each atom in Table 1, except that when the individual *B_{ii}* varied by more than a factor of 2 we have given the approximate direction(s) of maximum apparent vibration. These average values can be plausibly interpreted in terms of the structure and packing of the molecules and will be discussed later.

One cycle of differential Fourier synthesis was calculated, as indicated in Fig. 2, with parameter Set 15, just before the last two least squares cycles. Because the routine is limited to calculations at the positions of 20 atoms, the observed and calculated electron densities and their slopes and curvatures were evaluated only at the positions of the twenty C, N, and O atoms of the thymidylate ion, and not for the Ca, P, or six water oxygens. No shift in position as large as 0.005 Å was indicated, and since this was less than one-half the e.s.d. of the position of any of these atoms, no shifts were made. The average value of the ratio of the observed to calculated curvature of the electron density was 0.993, but there was appreciable individual variation (maximum spread of 6% for $\partial^2\rho/\partial x^2$, 11% for $\partial^2\rho/\partial y^2$, and 4% for $\partial^2\rho/\partial z^2$). This variation is not surprising in view of the known absorption errors and indeed it is another indication of the inadequacies of our individual derived 'temperature factors'. An attempt to refine temperature factors by differential Fourier methods might have yielded somewhat better values, but the data did not seem to merit the effort. It is noteworthy also that the observed peak heights were greater than those calculated by 3-4%, suggesting that the scale factor might be somewhat too high (at least for the temperature factors being used). On the other hand, the last five least squares cycles had suggested consistently that the scale factor was about 2% low, although because no cross-terms were calculated the indicated shift could not be considered of great significance and no shift was applied. The sums of F_o and of $|F_c|$ agreed within about 1%.

The final value of the usual discrepancy index, R , was 11.8% for the 1575 observed reflections (11.6% if the hydrogen atoms are included in the calculation). Although $|F_c|$ was larger than the estimated minimum observable F_o for 19 of the 211 unobserved reflections, it was as large as 1.5 F_{\min} . for only three of these, and for none was it as great as 2 F_{\min} . A complete list of h , k , l , F_o , $|F_c|$, $F_o \cos \alpha$, and $F_o \sin \alpha$ is presented in Table 7.

The e.s.d.'s of the atomic positions were estimated from the diagonal elements of the matrix of the least squares normal equations, a procedure which past experience has shown to give values only a few per cent higher than those estimated more rigorously from the inverse matrix. The difference is certainly not significant. The e.s.d.'s for the x and z coordinates (expressed in Å) were about the same for most atoms; those for the y coordinates averaged about 30% larger, occasionally being nearly twice as large. These individual variations were considered in calculation of the e.s.d.'s of bond distances and angles. The e.s.d.'s of atomic positions (in Å) were: 0.003 for Ca, 0.0035 for P, 0.010 to 0.014 for the eight oxygens of the molecule, 0.012 to 0.018 for the water oxygens, 0.013 for the nitrogens, and 0.014 to 0.019 for the carbons.

The structure of the thymidylate ion

In discussing the crystal structure, we shall consider first the different portions of the thymidylate ion separately, then the conformation of the ion as a whole, and finally the packing of the ions and water molecules which constitute the structure. Tables 3 and 4 list the bond distances and angles in the ion, with their e.s.d.'s; certain significant non-bonded intramolecular distances are listed also. The structure of

Table 3. Distances within the thymidylate ion*

N1-C2	1.377 (0.018)	C7 ... O6	2.90 (0.02)
C2-N3	1.365 (0.018)	C1' ... O2	2.74 (0.02)
N3-C4	1.367 (0.018)	C4 ... C2'	3.23 (0.02)
C4-C5	1.310 (0.022)	C4 ... O1'	2.77 (0.02)
C5-C6	1.452 (0.021)	C5' ... O _I	2.95 (0.02)
C6-N1	1.414 (0.018)	C5' ... O _{II}	3.14 (0.02)
C2-O2	1.247 (0.018)		
C5-C7	1.526 (0.023)	Ha on C5' ... O _I	2.9
C6-O6	1.218 (0.019)	... O _{II}	3.8
N3-C1'	1.466 (0.018)	Hb on C5' ... O _I	2.8
C1'-C2'	1.527 (0.028)	... O _{II}	2.6
C2'-C3'	1.550 (0.019)	Ha on C7 ... O6	2.8
C3'-C4'	1.491 (0.022)	Hb on C7 ... O6	2.7
C4'-O1'	1.441 (0.017)	Hc on C7 ... H on C4	2.5
O1'-C1'	1.438 (0.018)	H on C1' ... O2	2.5
C3'-O3'	1.409 (0.018)	H on C4 ... O1'	2.4
C4'-C5'	1.526 (0.022)		
C5'-O5'	1.472 (0.019)		
O5'-P	1.587 (0.011)		
P-O _I	1.486 (0.011)		
P-O _{II}	1.514 (0.011)		
P-O _{III}	1.474 (0.011)		

* The numbers in parentheses are the estimated standard deviations. Units are Å throughout.

Table 4. Bond angles in the thymidylate ion*

N1-C2-N3	115.8°	C1'-C2'-C3'	103.3
N1-C2-O2	120.8	C2'-C3'-C4'	101.8
N3-C2-O2	123.2	C2'-C3'-O3'	114.3
C2-N3-C4	121.4	C4'-C3'-O3'	113.7
C2-N3-C1'	117.6	C3'-C4'-O1'	106.7
C4-N3-C1'	121.0	C3'-C4'-C5'	117.1
N3-C4-C5	123.3	O1'-C4'-C5'	107.6
C4-C5-C6	120.3	C4'-O1'-C1'	108.9
C4-C5-C7	124.5	C4'-C5'-O5'	109.4
C6-C5-C7	115.1	C5'-O5'-P	118.8
C5-C6-N1	113.4	O5'-P-O _I	107.6
C5-C6-O6	128.8	O5'-P-O _{II}	107.6
N1-C6-O6	117.7	O5'-P-O _{III}	102.1
C6-N1-C2	125.7	O _I -P-O _{II}	106.0
N3-C1'-C2'	115.0	O _I -P-O _{III}	118.4
N3-C1'-O1'	107.4	O _{II} -P-O _{III}	114.4
C2'-C1'-O1'	107.2		

* Estimated standard deviations are about 0.7° for O-P-O angles, 1.0° for C5'-O5'-P, and about 1.4° for the others.

the ion is illustrated in Figs. 7 and 8, which also show the probable hydrogen bonds in which the ion is directly involved.

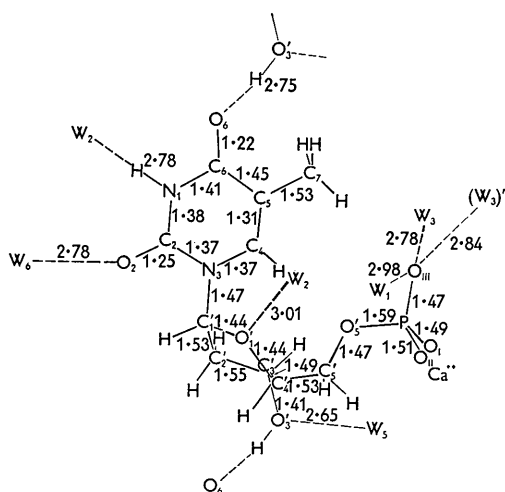


Fig. 7. Bond distances in the thymidylate ion and possible hydrogen bond distances directly involving this ion. The view is along the positive direction of **b**.

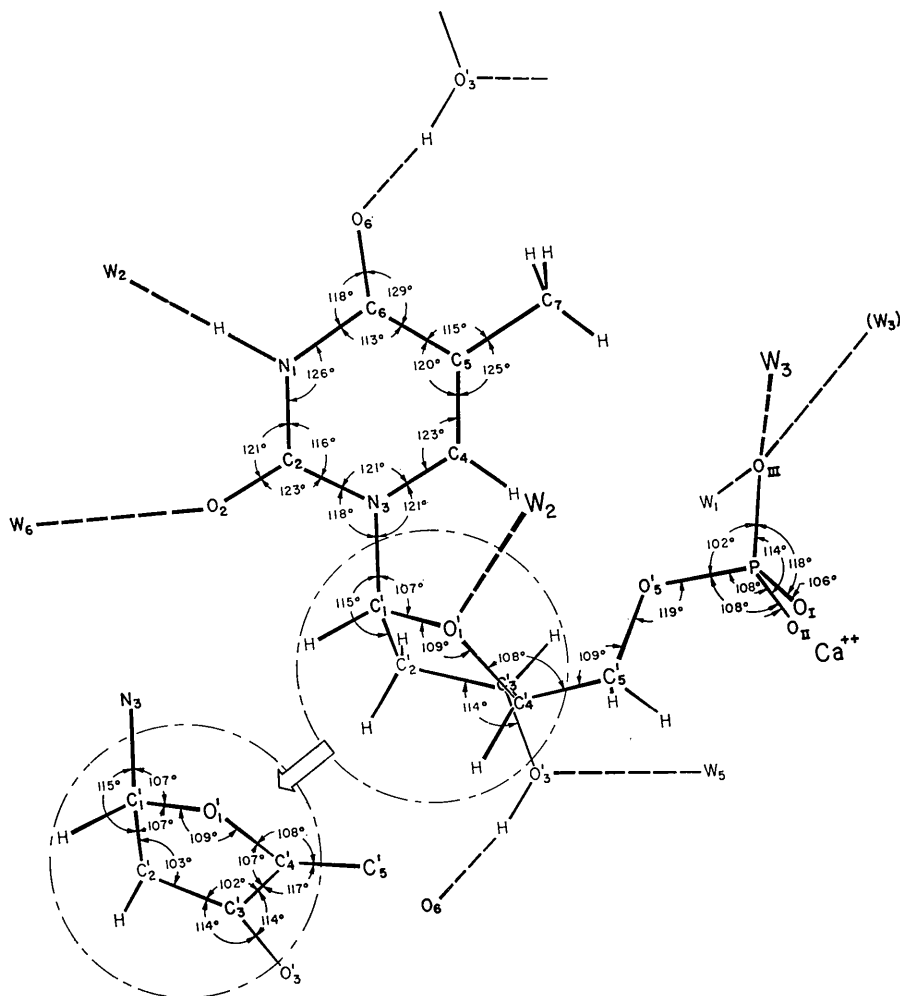


Fig. 8. Bond angles in the thymidylate ion. The view is along the positive direction of **b** except for the insert which shows the deoxyribose ring viewed from a more convenient direction.

The thymine ring

The configuration found for the thymine nucleus is compared in Fig. 9 with those predicted by Spencer (1959a) and Pauling & Corey (1956) in their consideration of models of DNA. A precise determination of the structure of thymine itself (as the monohydrate) has recently been made by Gerdil (1961). His results, which are more precise than ours, agree generally well with ours. The only distance which differs by more than 1 e.s.d. is C4-C5, for which he finds 1.35 Å, a more plausible value than our 1.31 Å. The largest deviation in an angle is for C6-C5-C7, for which Gerdil found 119° as contrasted with our 115°; no other angle deviates more than about 2°. We know of no other structural studies of thymine derivatives, although the structure of the related substance, uracil (which has a hydrogen atom in place of the methyl group of thymine) has been determined by Parry (1954). Even if allowance is made for the fact that his e.s.d.'s are probably underestimated by a factor of at least

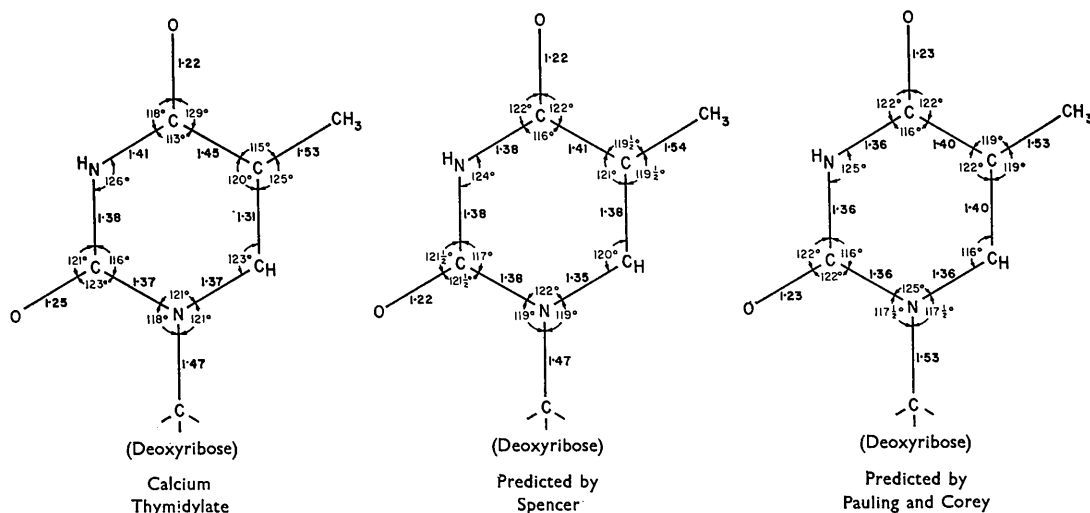


Fig. 9. Structures of the thymine residue (a) found in calcium thymidylate, (b) predicted by Spencer (1959a), (c) predicted by Pauling & Corey (1956).

two because so large a proportion of the reflections were weak (Sparks, 1958), one major discrepancy with our results, and with Gerdil's, remains. Parry finds the C4-C5 distance to be 1.41 Å; it is of course possible that there is a real difference between thymine and

uracil here, although it seems unlikely that it would be so large. The two studies of thymine and that of uracil agree on one important point: the C2-O2 and C6-O6 distances are so nearly the same as those characteristic of ketones and aldehydes (average 1.23 Å, Sutton, 1958) that there can be no question concerning the tautomeric form of the molecules in the crystals. They are in the keto, not the enol, form.

The only significant differences between the geometry of the thymine residue as observed by us (and by Gerdil) and that predicted recently by Spencer (1959a) are in the region of C5 and C6. The C4-C5 bond seems to be more nearly a pure double bond than predicted, with the angles at C5 in accord with this view. The C5-C6 bond is somewhat longer than predicted, and is indeed about twice the expected radius (0.73 Å) for trigonally hybridized carbon (Dewar & Schmeising, 1959). The bond angles at C6 are significantly distorted, presumably chiefly as a result of the short non-bonded intramolecular contact between the methyl group (C7) and O6 (see Table 3). The distortion of the angles increases this distance by about 0.1 Å.

All six atoms of the pyrimidine nucleus lie in the same plane (plane I of Table 5), the maximum deviation being less than the e.s.d. of an atomic position. The displacements of C7 and O6 from this plane are significant and are equal in magnitude and opposite in direction; presumably this results also from the close C7...O6 contact. The displacements of O2 and C1' from the plane of the ring are also significant and opposed, although the former atom is about twice as far from the plane as the latter.

The sugar

The deoxyribose ring may be described in various alternative ways. Least-squares planes were calculated for all five atoms of the ring and for all possible

Table 5. *Some least-squares planes**

Plane	Atoms comprising the plane	Displacements	Displacements of other atoms	Angles of plane normal†	
I	N1	-0.003 Å	O2	0.101	88.7°
	C2	-0.004	C1'	-0.050	
	N3	-0.012	C7	0.061	84.1
	C4	0.009	O6	-0.064	
	C5	0.008	C2'	1.27	
	C6	0.007	O1'	-1.01	
II	C1'	0.021	C3'	-0.53	49.7°
	C2'	-0.013	C5'	-0.73	110.5
	C4'	0.014	O3'	-0.13	
	O1'	-0.022	N3	-1.10	47.4
III‡	Ca	-0.07	W4	2.25	35.3°
	W1	0.08	W5	-2.41	92.3
	O _{IA}	-0.05			54.8
	O _{I_{IIA}}	-0.03			
	O _{IB}	0.01			
	O _{I_{IB}}	0.07			
IV	P	—	Ca	3.56	91.1°
	O5'	—	O _I	-1.04	17.4
	C5'	—	O _{II}	1.33	72.6
			O _{III}	-0.19	
			C4'	0.60	

* All planes were calculated in a manner similar to that described by Schomaker, Waser, Marsh & Bergman (1959).

† For each plane the three values listed are, respectively, the angles with the positive directions of **a***, **b**, and **c**.

‡ These atoms are those involved in the angles shown in Fig. 10; see also the footnote to Table 6.

combinations of four atoms in the ring. One of the latter combinations (plane II in Table 5) was far more satisfactory than the others. Atoms C1', C2', C4', and O1' are essentially coplanar, with C3' 0.53 Å from this plane; O3' is only 0.13 Å from the plane. Spencer (1959a) correctly anticipated this puckering, stating that either C2' or C3' should lie out of the plane of the other ring atoms by about 0.5 Å.

The only bond distance in the sugar that differs appreciably from the expected value is that between C3' and C4', observed to be 1.49₁ Å. The 'normal' value is about 1.53₃ Å (Bartell, 1959) and thus the discrepancy is less than twice the e.s.d. and so cannot be considered significant. With certain exceptions the bond angles are close to the average values predicted by Spencer from a survey of similar molecules—internal angles of 105° and 108° at C and O atoms respectively, and external angles of about 112° at carbon. Two of the angles deviate from the latter value by as much as 5°; if the effect is real, it is not especially surprising for angle deformation requires comparatively little energy. For an average force constant, a 5° bend would require only about 0.7 kg.cal./mole. The exigencies of packing in so complex a molecule could readily provide energies of this magnitude.

The phosphate group

The phosphorus-oxygen distances in the phosphate group are in general accord with expectation, although there are no precise distances in similar molecules for comparison. The ester bond is much the longest of the four and that to the oxygen with no formal charge is the shortest, although its difference from one of the two bonds to the formally negative oxygens is only about 1 e.s.d. Whether the difference between the P-O_I and P-O_{II} distances is real is questionable; it is, however, at about the 99% significance level if one accepts the e.s.d.'s calculated in the usual way on the assumption that the errors are random. It is noteworthy that the shorter distance (P-O_I) involves the oxygen which is further from both of the calcium ions to which each of these oxygens is coordinated (Fig. 10); this would tend to produce an effect in the observed direction but it may be mere coincidence.

The only precise published determination of the structure of an organic phosphate is that of dibenzyl phosphoric acid (Dunitz & Rollett, 1956). In this molecule, however, there are two ester P-O bonds and one P-OH bond, the lengths being 1.57, 1.55, and 1.55 Å respectively; the fourth bond length is 1.47 Å. The bond angles at the ester oxygen atoms (O₅' in the present structure) are 119° and 122°, in good agreement with the present value of 119°. Chemically equivalent O-P-O angles differ by 5° and 6°, these deviations being attributed to short non-bonded C...O contacts, which in the least favorable case differ by only 0.1 Å across the chemically equivalent angles. In the present molecule, the relatively short contacts

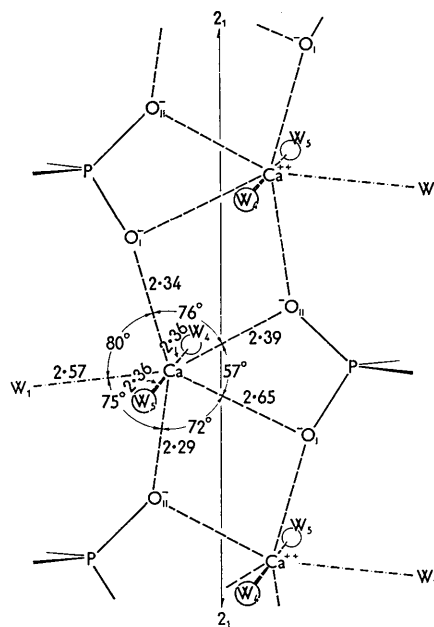


Fig. 10. Coordination of calcium ions with phosphate groups and water molecules.

of C5' with O_I and O_{II} (Table 3) may serve to enlarge the corresponding angles (O5'-P-O_I and O5'-P-O_{II}) somewhat at the expense of the angle on the opposite side (O5'-P-O_{III}), although if the above-cited explanation for dibenzyl phosphoric acid is correct one might have expected some difference in the O5'-P-O_I and -O_{II} angles to result from the 0.19 Å difference in the non-bonded contacts. The relatively large values of the O_{III}-P-O_I and O_{III}-P-O_{II} angles are to be expected from consideration of the electrostatic repulsion of lone pairs and bonding pairs of electrons near these atoms (Gillespie & Nyholm, 1957). Although

Table 6. Angles in suggested hydrogen-bonding scheme and calcium coordination not shown in Fig. 10 or 12*

At atom	Subtended by	Angle	At atom	Subtended by	Angle
W1	O _{III} , W2	95°	Ca ⁺⁺	W4, O _{IA}	80°
	O _{III} , W3	58		O _{IIA}	96
W3	O _{III} , W1	97°	O _{IB}	97	
		102	O _{IIB}	88	
		119	W1	82	
			W5	173	
W6	O2, W4	134°	W5, O _{IA}	O _{IA}	95°
	W3, W5	112		O _{IIA}	91
				O _{IB}	83
				O _{IIB}	87
				W1	102

* O_{IIIB} is related to O_{III} by the 2₁ at 0, y, $\frac{1}{2}$. O_{IA} and O_{IIA} are respectively above and below the calcium ion (Fig. 10). O_{IB} and O_{IIB} are opposite the calcium ion, across the 2₁ (Fig. 10). Since O_{IA}, O_{IIA}, O_{IB}, O_{IIB}, W1, and Ca⁺⁺ are essentially coplanar, the angle subtended at the calcium ion by any non-adjacent pair of the first five atoms may be calculated merely by summation of the angles given in Fig. 10.

in an isolated ion, or one in a more isotropic environment, one might expect the $O_{II}-P-O_{III}$ angle to be the largest of all for similar reasons, the presence of the calcium ion in the median plane of the phosphate group across the two-fold screw axis (Fig. 10) may act to decrease this angle significantly. (The calcium ions above and below will have much less effect on the bond angle because the corresponding Ca-O lines are much more nearly parallel to than perpendicular to the P-O bonds.)

Calcium ion environment

Fig. 10 depicts the packing of the phosphate groups and calcium ions, together with the water molecules directly coordinated with the latter. Each calcium ion has seven-fold coordination, with four phosphate oxygens (from three different molecules) and one water molecule lying approximately in a plane (Table 5), and two other waters on a line through the calcium nearly perpendicular to this plane (Table 6). This calcium environment is remarkably similar to that for one of the two non-equivalent calcium ions in $CaHPO_4$ (MacLennan & Beever, 1955), where the seven Ca-O distances range from 2.29 to 2.69 Å with an average value of 2.44. In the present structure, the range is almost the same (Fig. 10), with the average being 2.42 Å. The coordination number of calcium varies in different structures, with, as expected, smaller average distances for lower coordination number. For example, in $Ca(OH)_2$ (Busing & Levy, 1957), with six oxygens around each calcium, the Ca-O distance is 2.37 Å; for 8-fold coordinated calcium the average distance is about 2.5 Å (2.49 in $CaHPO_4$; 2.52 in $Ca(H_2PO_4)_2 \cdot H_2O$, MacLennan & Beever, 1956).

Conformation of the thymidylate ion

One of the most interesting structural parameters is the conformation about the glycosidic C-N bond. Fig. 11 presents schematic views along this bond for the thymidylate ion in the present structure, as well as for the original Crick-Watson (1954) model of DNA and the revision of that model by Langridge *et al.* (1957). In discussing this conformation, it is convenient (Donohue & Trueblood, 1960) to define a torsion angle, φ_{CN} , as the angle formed by the trace of the plane of the base with the projection of the $C1'-N$ bond. This angle, illustrated in Fig. 11, is taken as zero when $O1'$ is *anti-planar* to $C2$ of the pyrimidine or purine ring, and positive angles are taken as those measured in a clockwise direction when viewing from $C1'$ to N.

Fig. 11 shows that the torsion angle in the thymidylate ion lies about midway between the value proposed originally for DNA by Crick & Watson (1954) and the revised value of Langridge *et al.* (1957). Inspection of molecular models suggests that the difference between these three values is not significant in terms of non-bonded contacts. As has been discussed

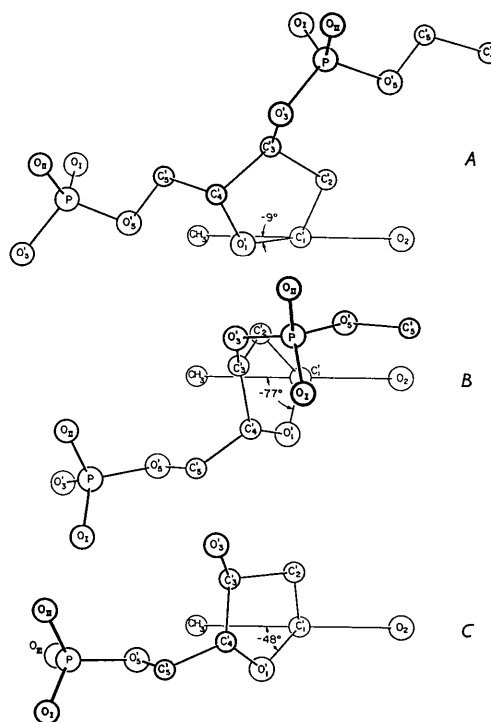


Fig. 11. Views showing the conformation about the glycosidic $C1'-N3$ bond viewed from C to N along the bond. A, the structure of DNA according to Crick & Watson, 1954; B, the structure of DNA according to Langridge *et al.*, 1957; C, the thymidylate ion. The angles shown are the values of φ_{CN} , defined in the text.

elsewhere (Donohue & Trueblood, 1960), consideration of molecular models suggests that there are two ranges of φ_{CN} within which relatively stable conformations might be assumed. Each of these ranges covers more than 90° , one being centered about *ca.* -30° (the *anti* range) and the other about *ca.* 150° (the *syn* range). Spencer (1959b) has noted that only the *anti* conformation, as here defined, has yet been observed in the three natural and synthetic pyrimidine nucleosides previously studied. The present structure provides another example of a natural *anti* conformation, but it is noteworthy that none of the structures so far reported involves a purine nucleotide. It may be significant that the only purine nucleoside whose structure has been reported, a cyclic adenosine nucleoside (Zussman, 1953) has the *syn* conformation; this is not a naturally occurring material, but the ease with which it is formed indicates that, at least with adenosine, the *syn* conformation is not difficult to achieve.

The plane of the three atoms $C5'-O5'-P$ in the thymidylate ion (IV in Table 5) has been rotated some 80° from the position assumed by Crick & Watson, essentially normal to the plane of the base, to a position in which it makes an angle of only about 12° with the plane of the base (Fig. 11). The situation of this chain of atoms in the present structure is rather

similar to that assumed in the model of Langridge *et al.* The difference from the Crick-Watson model involves rotation about the bonds C4'-C5' and O5'-P; in mononucleotides at least, this difference would not seem important energetically. The plane of the deoxyribose ring (II in Table 5) makes an angle of 75° with the plane of the pyrimidine nucleus. The general orientation is thus almost identical to that in cytidine, for which a value of 76° can be calculated from Furberg's (1950) parameters, and thus is very similar to that assumed by Crick & Watson in constructing their model.

Suggested hydrogen-bonding scheme and molecular packing

Fig. 12 shows the close contacts which might represent hydrogen bonds, and also the calcium ion-water bonds. The tentative hydrogen positions deduced from the difference map in accord with geometrical considerations are indicated also for the hydrogen atoms on the water molecules, as well as for those on N1 and O3'. If these suggested positions are correct,

only one of these fourteen hydrogen atoms (one of the two on W4) is not involved in a hydrogen bond. W4 has only one possible acceptor (W6) within a distance of 3.0 Å; the next nearest ones are O_I of the neighboring phosphate group across the *z*-axis (3.03 Å) and O_{II} of the phosphate group across the *x*-axis (3.28 Å). Each of these contacts is unusually long (Fuller, 1959) for a hydrogen bond from a water molecule to an oxygen atom in an anion; furthermore, no possible position for the second hydrogen on W4 is consistent with the shorter of these contacts if the W4-W6 contact is a hydrogen bond involving a hydrogen atom from W4, as seems likely. Thus it seems reasonably sure that W4 is involved in only one hydrogen bond.

There is only one apparent hydrogen bond in the structure which does not involve a water molecule, that from O3' to O6. The only other potential hydrogen-donor atom in the thymidylate ion, N1, forms a hydrogen bond with W2. The distances and angles in both of these contacts are normal (Fuller, 1959). The five water-water contacts range in distance from 2.74

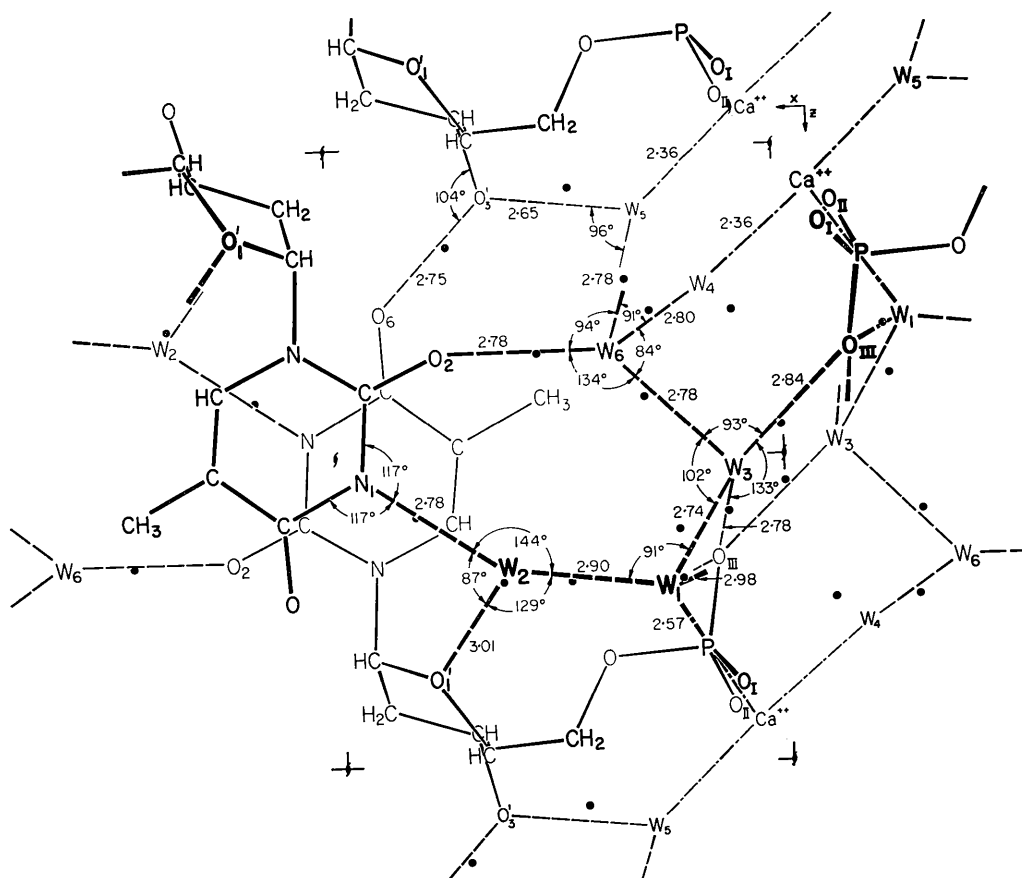


Fig. 12. Suggested scheme of hydrogen-bonding and calcium ion-water molecule coordination. The suggested positions (Table 2) for the hydrogen atoms on the water molecules and on N1 and O3' are indicated by black dots. Possible hydrogen bonds are shown by dashed lines and calcium ion-water molecule bonds by alternate dots and dashes. Pertinent angles not shown here are given in Table 6.

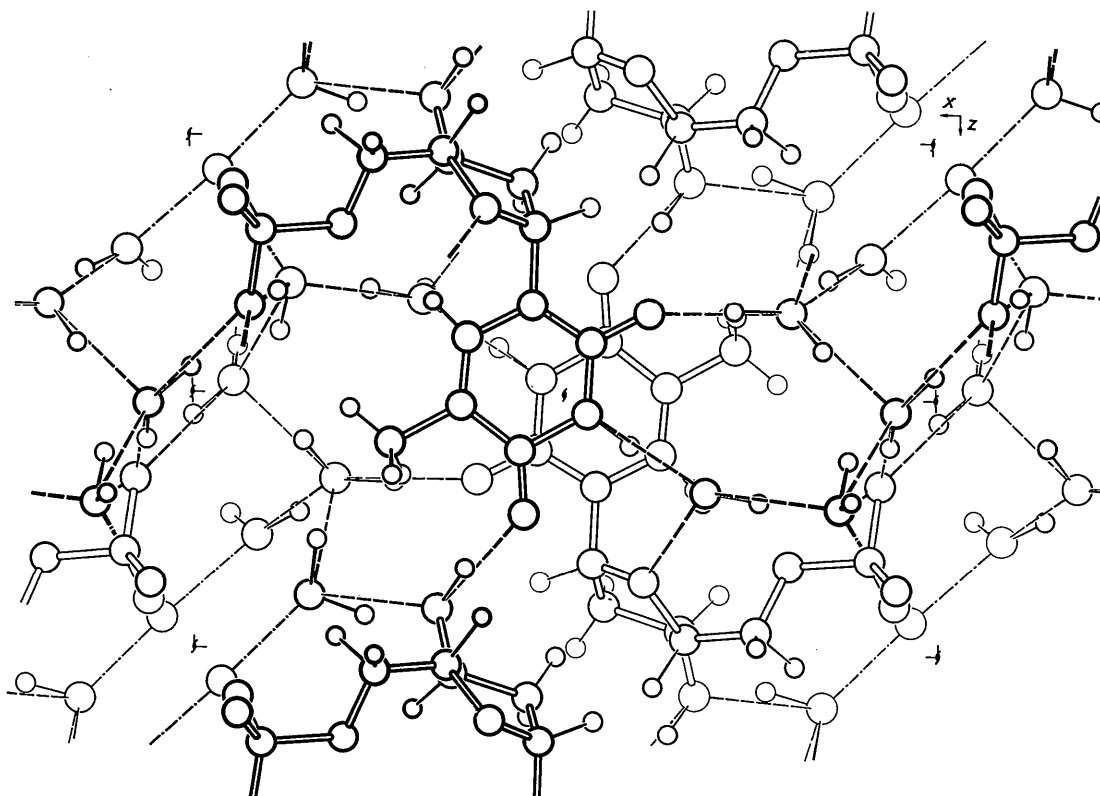


Fig. 13. A portion of the structure (slightly more than one unit cell) viewed along **b**. Atoms may be identified by comparison with Fig. 12. Hydrogen atoms are shown in the suggested positions of Table 2; these positions are at best tentative. Possible hydrogen bonds are shown by dashed lines and calcium ion-water molecule bonds by alternate dots and dashes.

to 2.90, with the average 2.80; presumably all or at least most of these involve hydrogen bonds. Bonds of this sort have been observed to vary in length from 2.64 to 2.91 Å, with the average of twenty values 2.75 Å (Fuller, 1959). Of the other possible hydrogen bonds, those from W3 to two different O_{III} atoms, from W6 to O2, and from W5 to O3' seem very plausible. On the other hand, identification of the contact from W2 to O1 as a hydrogen bond is questionable, both because of the rather long distance (3.01 Å), and the unfavorable suggested position for the corresponding hydrogen atom on W2. Similarly the contact between W1 and O_{III} is rather long (2.98 Å), although the suggested position of the hydrogen atom on W1 is consistent with the hypothesis that this contact involves a hydrogen bond.

Three of the six water molecules are bonded to the calcium ion; it is noteworthy (Table 1) that the apparent thermal motions of these three are lower than those for the other three water molecules, which are held in the structure only by hydrogen bonds. It seems significant also that the oxygen atom of W2 has the highest apparent thermal vibration amplitude of any atom in the structure; it is involved only in one strong hydrogen bond (with N1), the contacts with W1 and O1' being at best weak hydrogen bonds.

Fig. 13 is a drawing of a portion of the entire structure, including the hydrogen atoms in their suggested positions. Different thymidylate ions are in contact in two regions of the unit cell: the bases are stacked along the two-fold screw axis at $(\frac{1}{2}, y, \frac{1}{2})$, and the sugar rings approach each other around the screw axis at $(\frac{1}{2}, y, 0)$. If the planes of the bases were just normal to **b**, they would be parallel and separated by $b_0/2 = 3.44$ Å which is very nearly the value assumed by Crick & Watson (1954). However, in fact they are tipped slightly (Table 5), successive planes being at 12° to one another. Because of this tip, the closest approach is 3.20 Å, between C2 and C6 of successive residues. These atoms overlap slightly in the view along **b** in Fig. 13.

There are no unusually close contacts between the atoms of successive sugar rings related by the screw axis. The closest approach of any pair of 'heavy' atoms is 3.37 Å, from C2' of one ring to O1' of the next. Several of the suggested hydrogen positions imply rather short contacts: H on C1' to H(*a*) on C2', 2.0 Å, and to H on O3', 2.2 Å; H(*a*) on C2' to O1', 2.4 Å, and to H on C4', 2.4 Å. However, since even those hydrogen positions which are reasonably well established by virtue of the tetrahedral nature of the carbon atom could easily be in error by 0.1 Å, and that for the

Table 7 (cont.)

15	105	91	104	14	5	249	261	11	248	5	144	147	109	94	12	51	48	47	16	5	132	138	140	124	128	132	136	140	144	148	152	156	160	164	168	172	176	180	184	188	192	196	200	204	208	212	216	220	224	228	232	236	240	244	248	252	256	260	264	268	272	276	280	284	288	292	296	300	304	308	312	316	320	324	328	332	336	340	344	348	352	356	360	364	368	372	376	380	384	388	392	396	400	404	408	412	416	420	424	428	432	436	440	444	448	452	456	460	464	468	472	476	480	484	488	492	496	500	504	508	512	516	520	524	528	532	536	540	544	548	552	556	560	564	568	572	576	580	584	588	592	596	600	604	608	612	616	620	624	628	632	636	640	644	648	652	656	660	664	668	672	676	680	684	688	692	696	700	704	708	712	716	720	724	728	732	736	740	744	748	752	756	760	764	768	772	776	780	784	788	792	796	800	804	808	812	816	820	824	828	832	836	840	844	848	852	856	860	864	868	872	876	880	884	888	892	896	900	904	908	912	916	920	924	928	932	936	940	944	948	952	956	960	964	968	972	976	980	984	988	992	996	1000
----	-----	----	-----	----	---	-----	-----	----	-----	---	-----	-----	-----	----	----	----	----	----	----	---	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	------

H on O3' even more, these short apparent contacts are not inconsistent with the usual van der Waals radius for hydrogen, 1.1-1.2 Å. The only other apparent H-H contact of less than 2.4 Å is that between H(a) on C5' and H(a) on W5, 2.2 Å.

It has been emphasized above that the limitations of the data preclude any extensive discussion of anisotropic thermal motion in this structure. However, comparison of Figs. 10 and 13 with the gross indications of anisotropy included with the temperature

- LUZZATI, V. (1953). *Acta Cryst.* **6**, 142.
 MACLENNAN, G. & BEEVERS, C. A. (1955). *Acta Cryst.* **8**, 579.
 MACLENNAN, G. & BEEVERS, C. A. (1956). *Acta Cryst.* **9**, 187.
 MCWEENY, R. (1951). *Acta Cryst.* **4**, 513.
 MCWEENY, R. (1954). *Acta Cryst.* **7**, 180.
 PARRY, G. S. (1954). *Acta Cryst.* **7**, 313.
 PAULING, L. & COREY, R. B. (1956). *Arch. Biochem. Biophys.* **65**, 164.
 ROSSMANN, M. G., JACOBSON, R. A., HIRSHFELD, F. L. & LIPSCOMB, W. N. (1959). *Acta Cryst.* **12**, 530.
 SCHOMAKER, V., WASER, J., MARSH, R. E. & BERGMAN, G. (1959). *Acta Cryst.* **12**, 600.
 SPARKS, R. A. (1958). Ph.D. Thesis. Los Angeles: University of California.
 SPARKS, R. A., PROSEN, R. J., KRUSE, F. H. & TRUEBLOOD, K. N. (1956). *Acta Cryst.* **9**, 350.
 SPENCER, M. (1959a). *Acta Cryst.* **12**, 59.
 SPENCER, M. (1959b). *Acta Cryst.* **12**, 66.
 SUTTON, L. E. (editor), (1958). *Tables of Interatomic Distances and Configuration in Molecules and Ions*. London: The Chemical Society.
 WASER, J. (1944). Ph.D. Thesis. Pasadena: California Institute of Technology.
 WATSON, J. D. & CRICK, F. H. C. (1953). *Nature, Lond.* **171**, 737.
 WOLFSON, M. (1956). *Acta Cryst.* **9**, 974.
 ZUSSMAN, J. (1953). *Acta Cryst.* **6**, 504.

Acta Cryst. (1961). **14**, 982

The Structure Analysis of the T_3 (AlMnZn) Compound

BY A. DAMJANOVIC*

Crystallographic Laboratory, Cavendish Laboratory, Cambridge, England

(Received 27 May 1959 and in revised form 9 December 1960)

Of the three aluminium-rich intermetallic compounds, T_1 , T_2 and T_3 , which separate as primary constituents in the Al-Mn-Zn system, T_3 is shown to be structurally similar to $Ni_4Mn_{11}Al_{60}$ and $Cu_2Mn_3Al_{20}$, although it is T_1 which corresponds in composition and in electron concentration (e/a) with the latter two. In the final stage of the structure analysis of the T_3 compound, interatomic distances and the atomic environments had to be used as the criteria for determining the distribution of different atoms amongst some of the available sites. A possible explanation is given for the fixed composition of $Ni_4Mn_{11}Al_{60}$ and the varying composition of T_3 .

1. Introduction

In an examination of the Al-Mn-Zn system in the range from 0 to 95 wt. % of zinc and from 0 to 3 wt. % of manganese, Raynor & Wakeman (1947) found three aluminium-rich ternary phases, T_1 , T_2 and T_3 , which may crystallize as primary constituents from slowly cooled alloys. The structures of these phases were not known. The ideal formula of the T_1 phase is $ZnMn_5Al_{24}$. Its composition can be related to those of $Ni_4Mn_{11}Al_{60}$ and $Cu_2Mn_3Al_{20}$; it was suggested that the formation of all three phases is controlled to a considerable extent by two factors:

- (i) a ratio of four aluminium atoms to one atom of heavy element, and
- (ii) the attainment of a definite electron-to-atom ratio.

Robinson (1952a, 1954) has solved the structure of the $Ni_4Mn_{11}Al_{60}$ compound and has shown that the basic structure of $Cu_2Mn_3Al_{20}$ is essentially the same as that of $Ni_4Mn_{11}Al_{60}$, but that the structure of T_1 is appreciably different, its unit-cell dimensions being

related to, but different from, those of $Ni_4Mn_{11}Al_{60}$ and $Cu_2Mn_3Al_{20}$. In this paper it is shown that the structure of the ternary T_3 compound is essentially similar to that of $Ni_4Mn_{11}Al_{60}$, though its composition does not satisfy the above requirements for the formation of the compounds $Ni_4Mn_{11}Al_{60}$ and $Cu_2Mn_3Al_{20}$.

2. Preparation of crystals

For the preparation of alloys the following materials were used.

- (i) pure zinc presented by the Imperial Smelting Corporation, Ltd., of Avonmouth. The major impurities are lead and cadmium, but both in quantity less than 0.0007%,
- (ii) super-purity aluminium kindly presented by the British Aluminium Co. Ltd., and
- (iii) aluminium-manganese master alloy containing 13.65 wt. % of manganese. The alloy was prepared from the super-pure elements by the British Aluminium Co. Ltd.

Ingots of about 50 g. were prepared by melting together in a sintered alumina crucible weighed-out quantities of aluminium and aluminium-manganese

* Now at the Faculty of Technology, University of Belgrade.